

# A systems approach to biology

SB200

Lecture 6

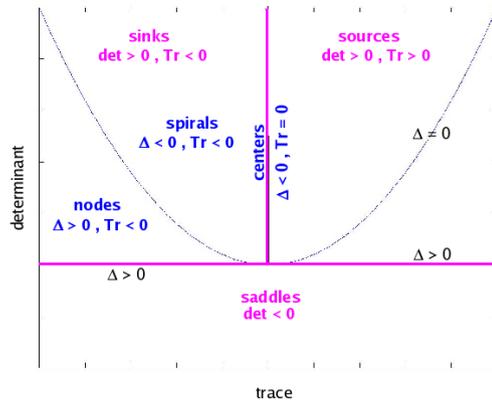
2 October 2008

Jeremy Gunawardena

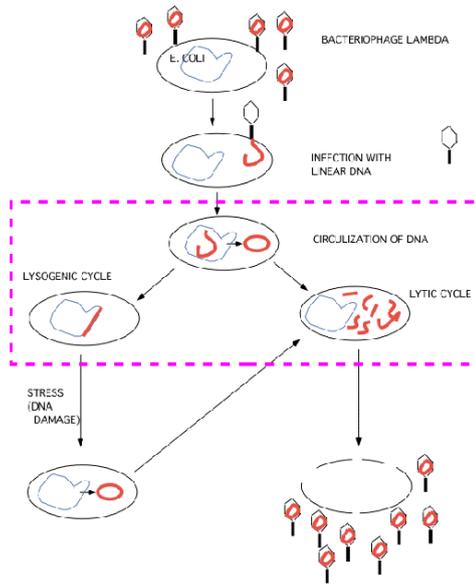
*jeremy@hms.harvard.edu*

# Recap of Lecture 5

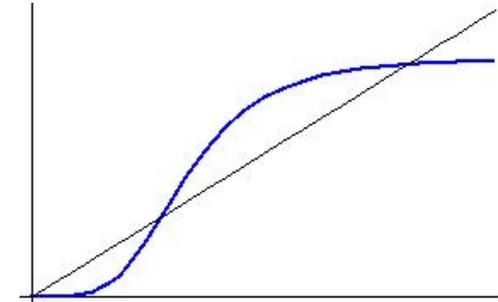
## Det/Tr diagram



## off state is unstable

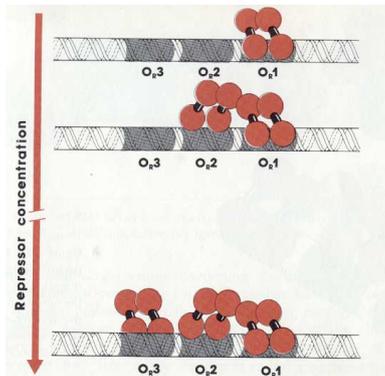


## sigmoidal dose response gives a stable off state and sharper on-to-off switching

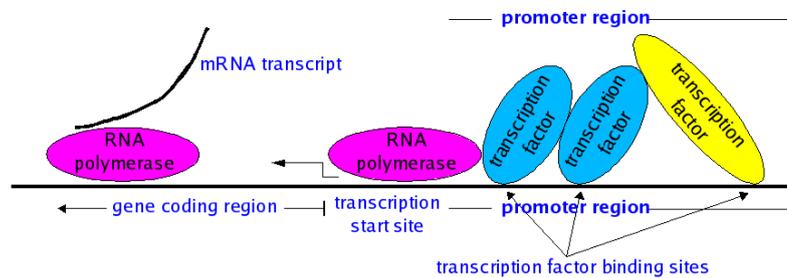


**SIGMOIDAL SWITCHING**  
**THRESHOLDING**  
**ULTRASENSITIVE**  
**ALLOSTERY**  
**COOPERATIVITY**

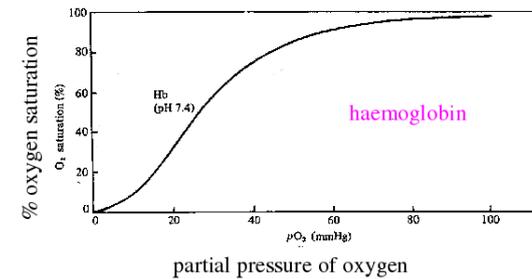
## $\lambda$ promoter



## bacterial gene expression



## oxygen curve for haemoglobin

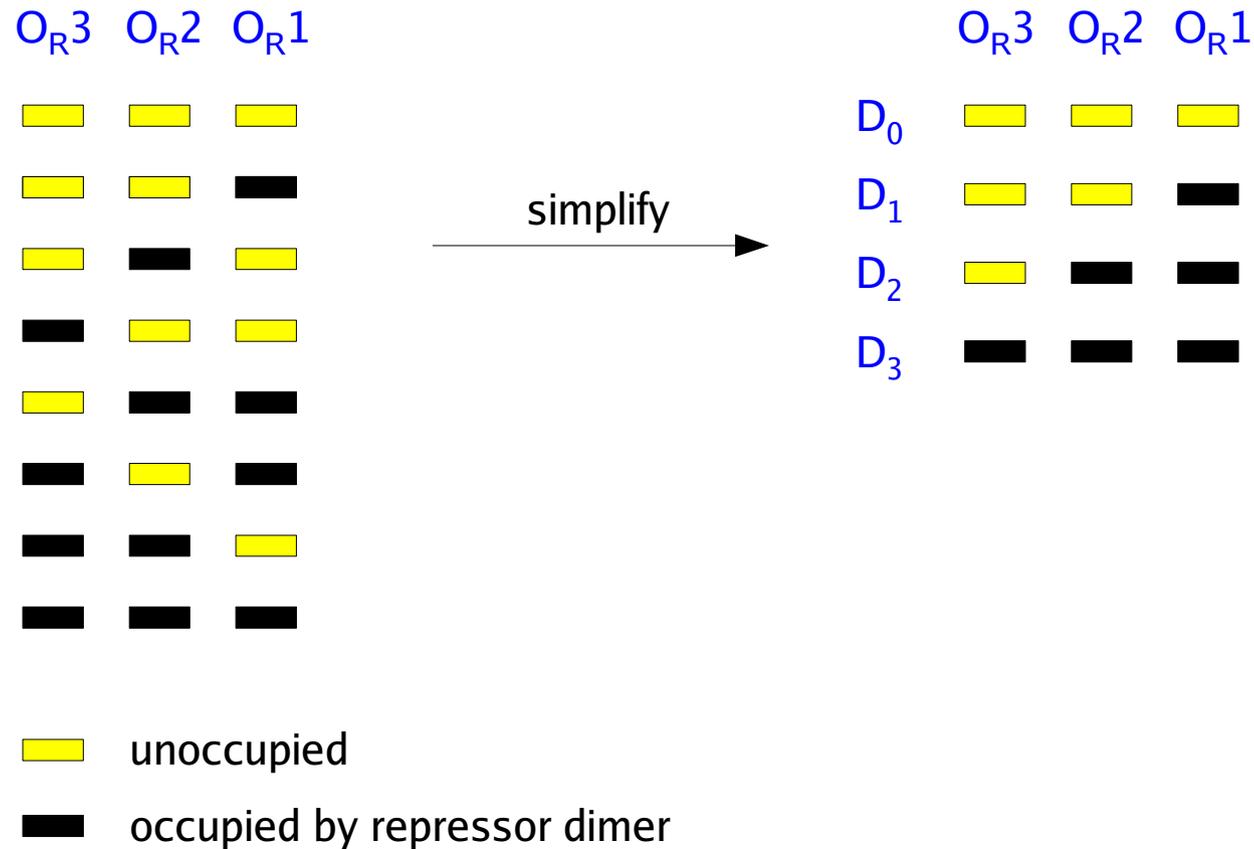


# calculating the rate of repressor expression

## Shea-Ackers model

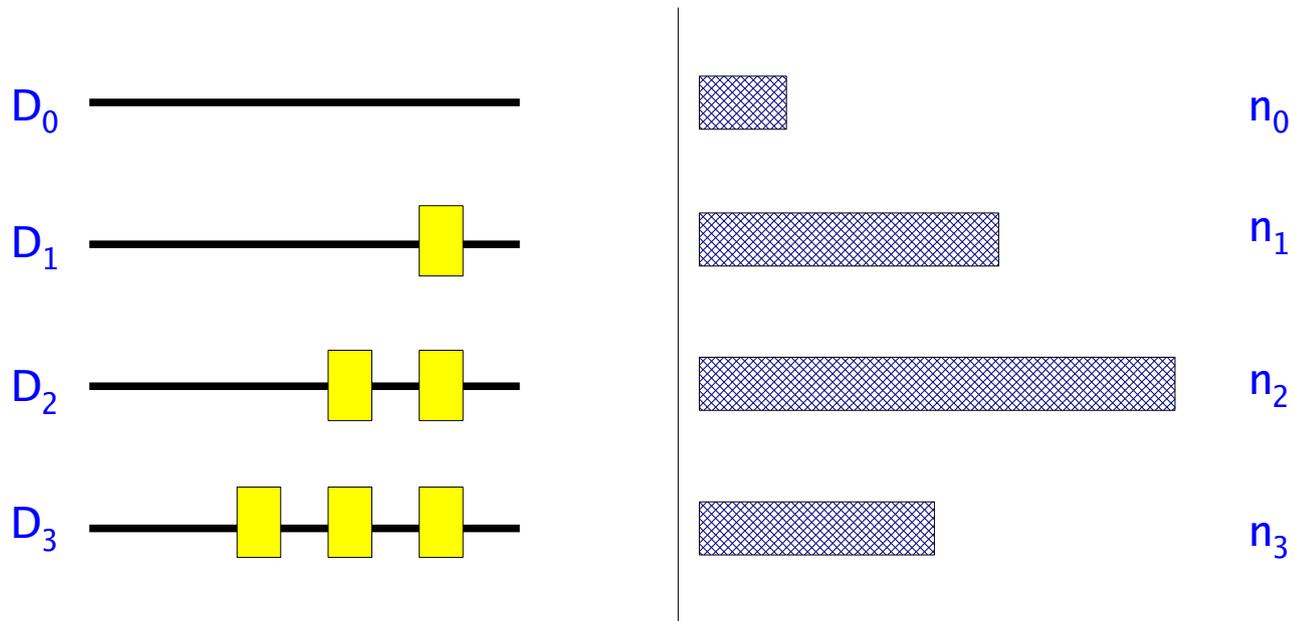
Ackers, Johnson & Shea, PNAS 79:1129-33 1982

a general statistical mechanical model for transcription factor binding



# probabilities as mean frequencies of occupation

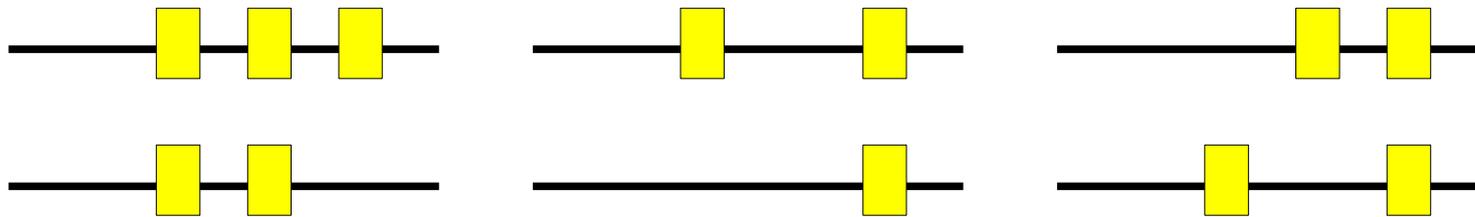
observe DNA over time and determine the occupation histogram



$$\text{probability}(D_i) = n_i / (n_0 + n_1 + n_2 + n_3)$$

## probabilities as concentration ratios

observe many copies of DNA in equilibrium with repressor and determine concentrations of each state ( $D_0$ ,  $D_1$ ,  $D_2$ ,  $D_3$ )



$$\text{probability}(D_i) = [D_i] / ([D_0] + [D_1] + [D_2] + [D_3])$$

the two ways of calculating probabilities give the same results (“ergodicity”)

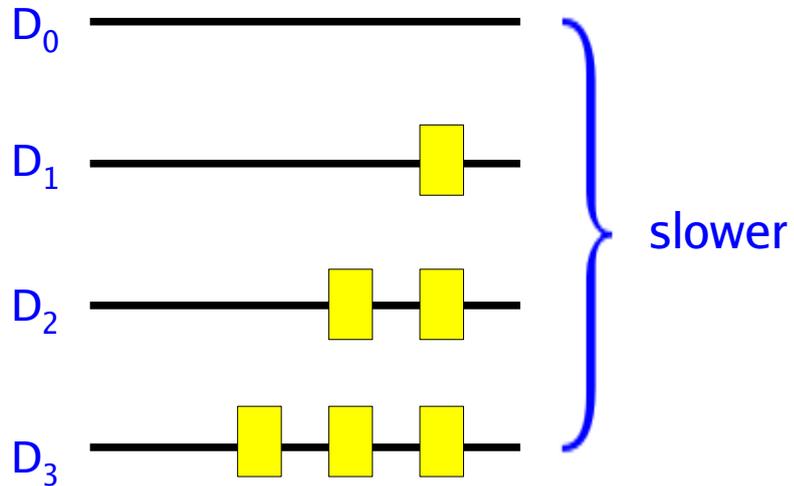
## separation of time scales



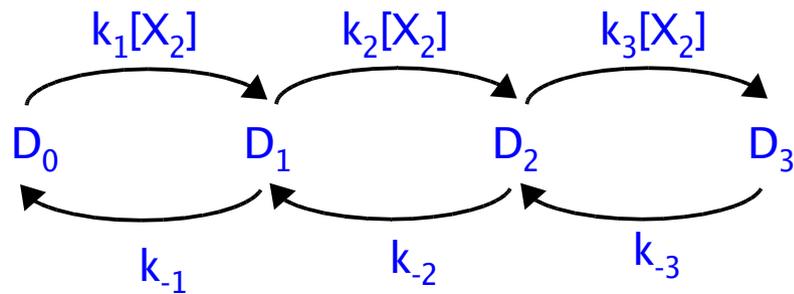
fast

$$[X_2] = K [X]^2$$

equilibrium constant



*assume repressor dimerisation is at equilibrium  
with respect to repressor-DNA binding*



*if a chain is at equilibrium, each individual loop is at equilibrium*

$$[D_i] = (k_i[X_2] / k_{-i}) [D_{i-1}]$$

$$K_i = k_i / k_{-i} \quad \text{equilibrium constant} \quad (M^{-1})$$

JG, Multisite protein phosphorylation makes a good threshold but can be a poor switch,  
PNAS **102**:14617-22 2005

$$[D_1] = K_1 [X_2][D_0] \quad [D_2] = K_1 K_2 [X_2]^2 [D_0] \quad [D_3] = K_1 K_2 K_3 [X_2]^3 [D_0]$$

$$[D_0] + [D_1] + [D_2] + [D_3] = [D_T]$$

$$[X_2] = K[X]^2$$

if  $r_i$  = transcription rate in state  $D_i$  then  
the average transcription rate  $r$  is

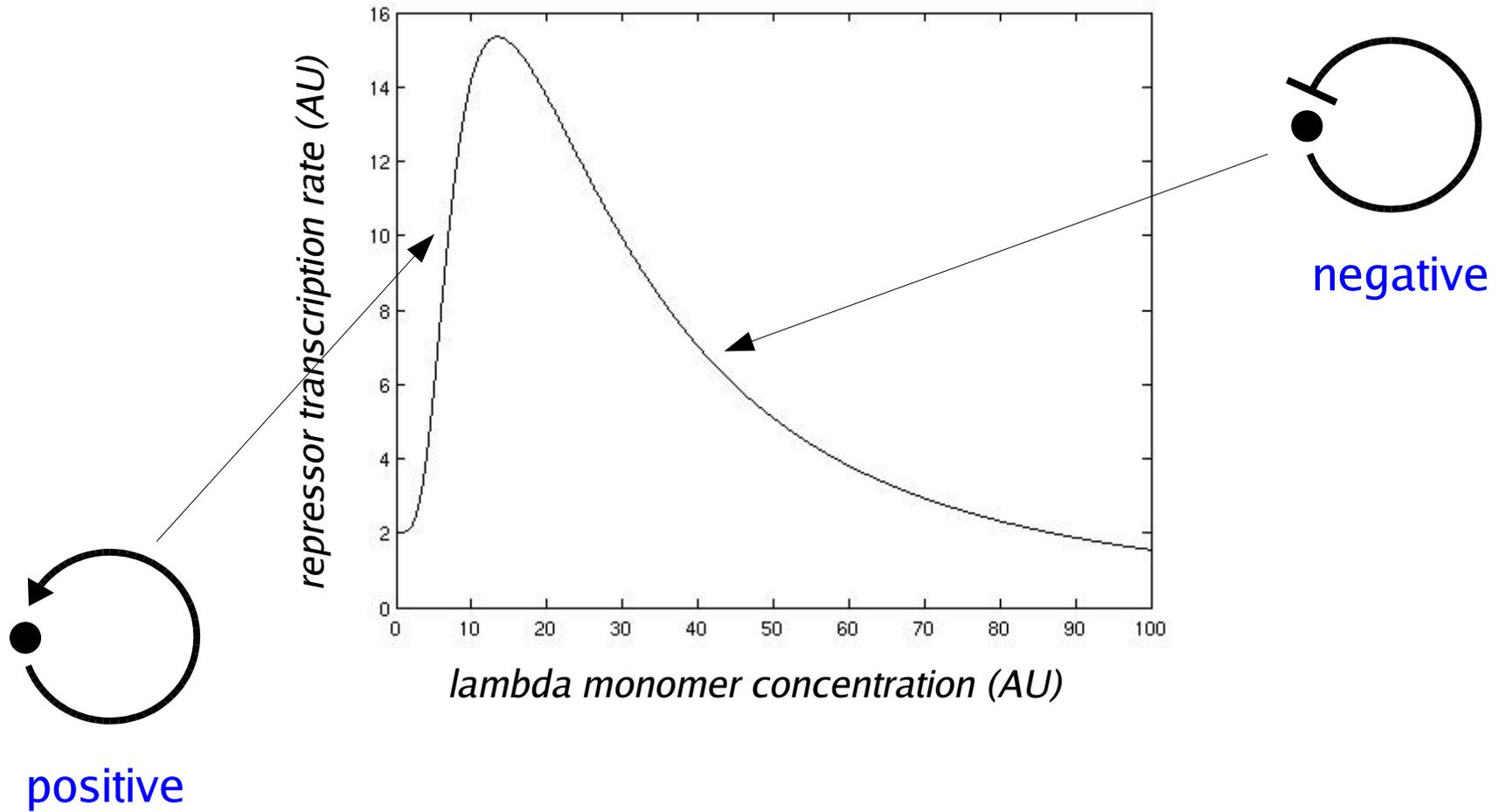
$$r = r_0 \frac{[D_0]}{[D_T]} + r_1 \frac{[D_1]}{[D_T]} + r_2 \frac{[D_2]}{[D_T]} + r_3 \frac{[D_3]}{[D_T]}$$

$$r = \frac{r_0 + r_1(K_1K)x^2 + r_2(K_1K_2K^2)x^4 + r_3(K_1K_2K_3K^3)x^6}{1 + (K_1K)x^2 + (K_1K_2K^2)x^4 + (K_1K_2K_3K^3)x^6}$$

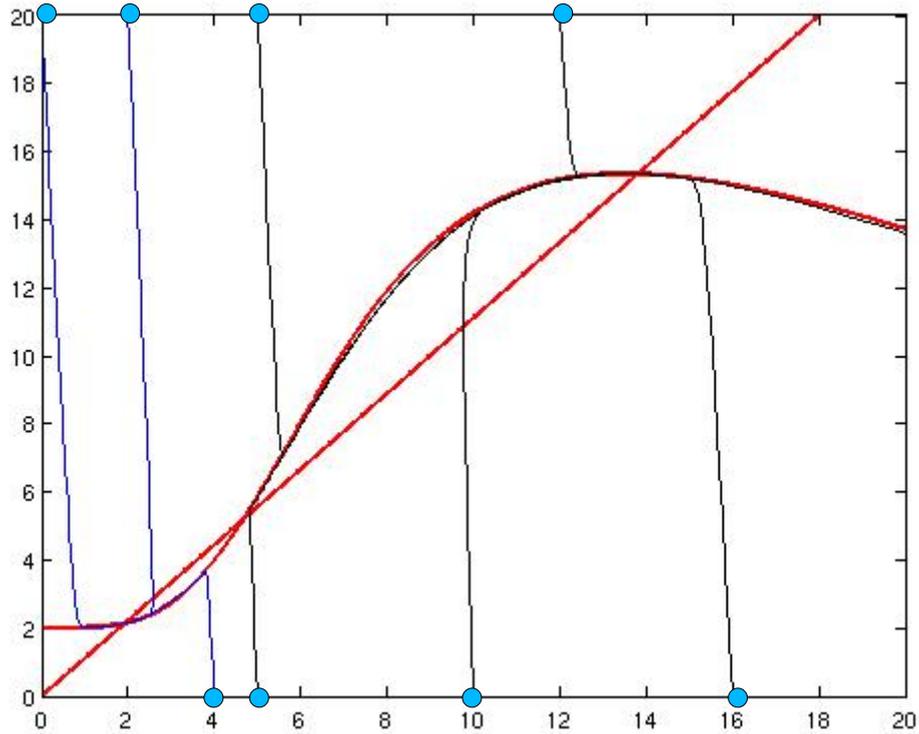
$r_0$ = basal transcription rate	$K = 5 * 10^7 \text{ M}^{-1}$
$r_1 = r_0$	$K_1 = 3.3 * 10^8 \text{ M}^{-1}$
$r_2 = 11 * r_0$	$K_2 = 2 * K_1$
$r_3 = 0$	$K_3 = 0.08 * K_1$

Ackers, Johnson & Shea, PNAS 79:1129-33 1982

# feedback is context dependent



# cooperative promoter design leads to bistability

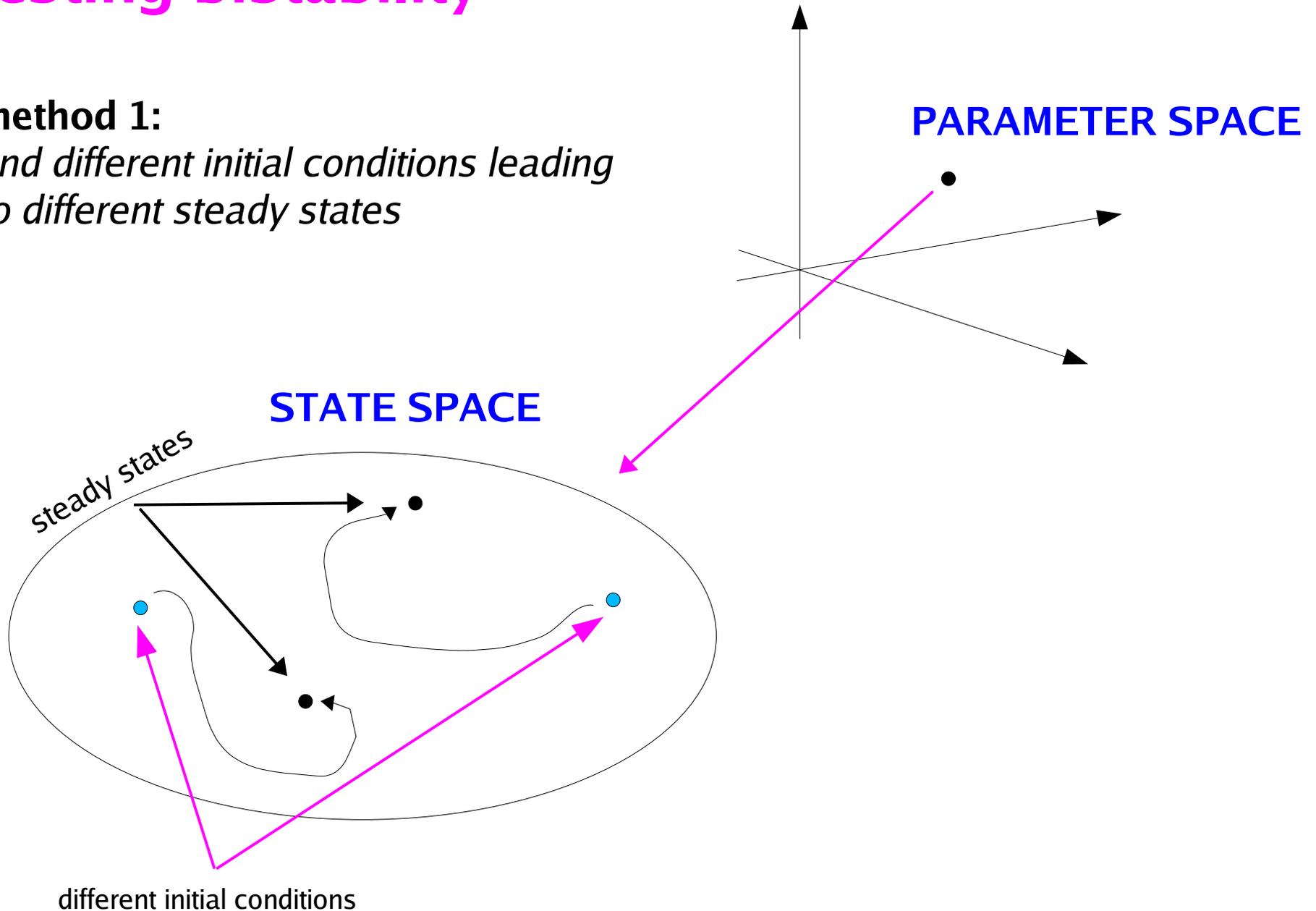


$\lambda$	0.18	(min) <sup>-1</sup>
a	0.02	(min) <sup>-1</sup>
b	0.5	(min) <sup>-1</sup>
$r_0$	1	(nM)(min) <sup>-1</sup>

# testing bistability

## method 1:

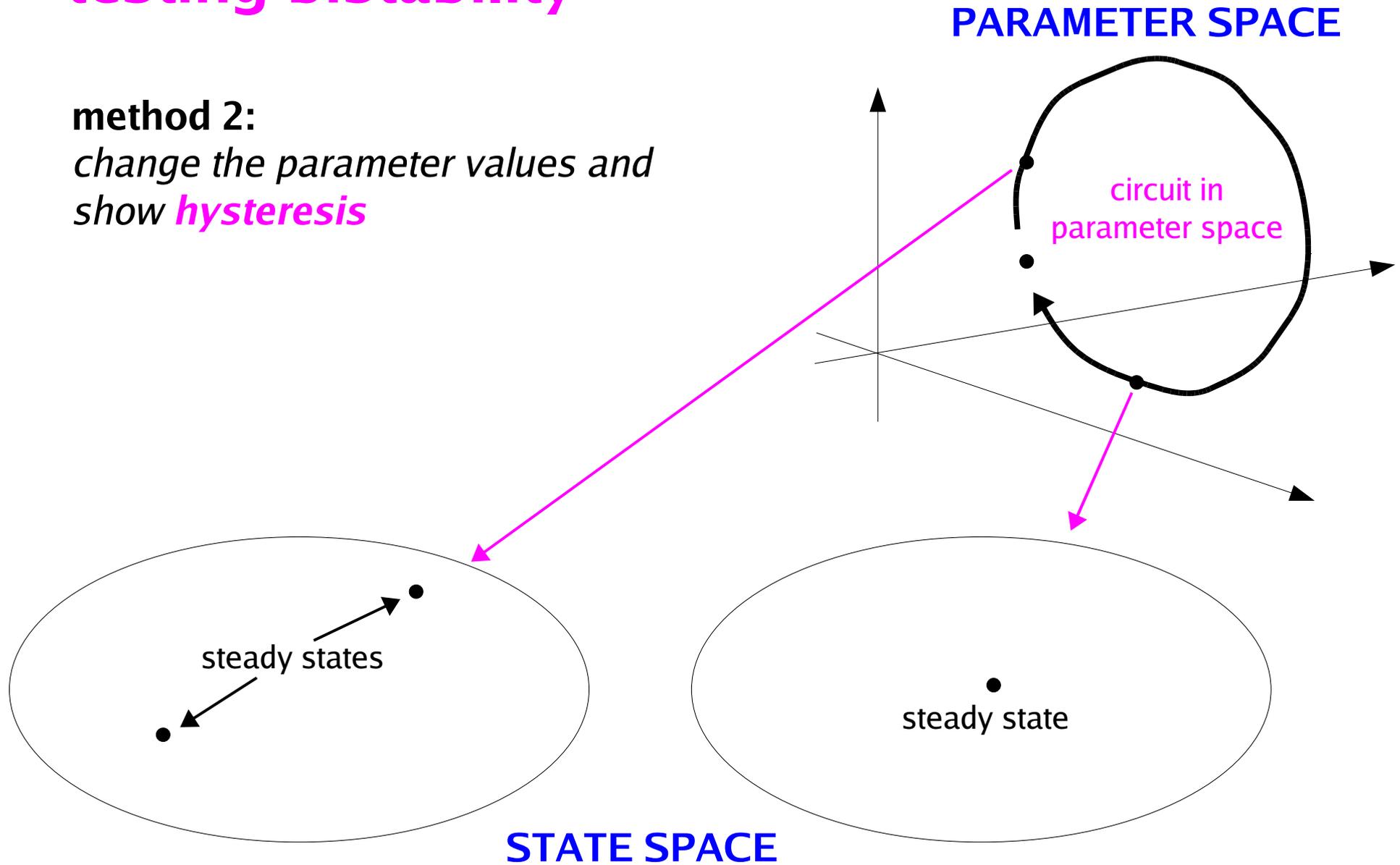
*find different initial conditions leading to different steady states*



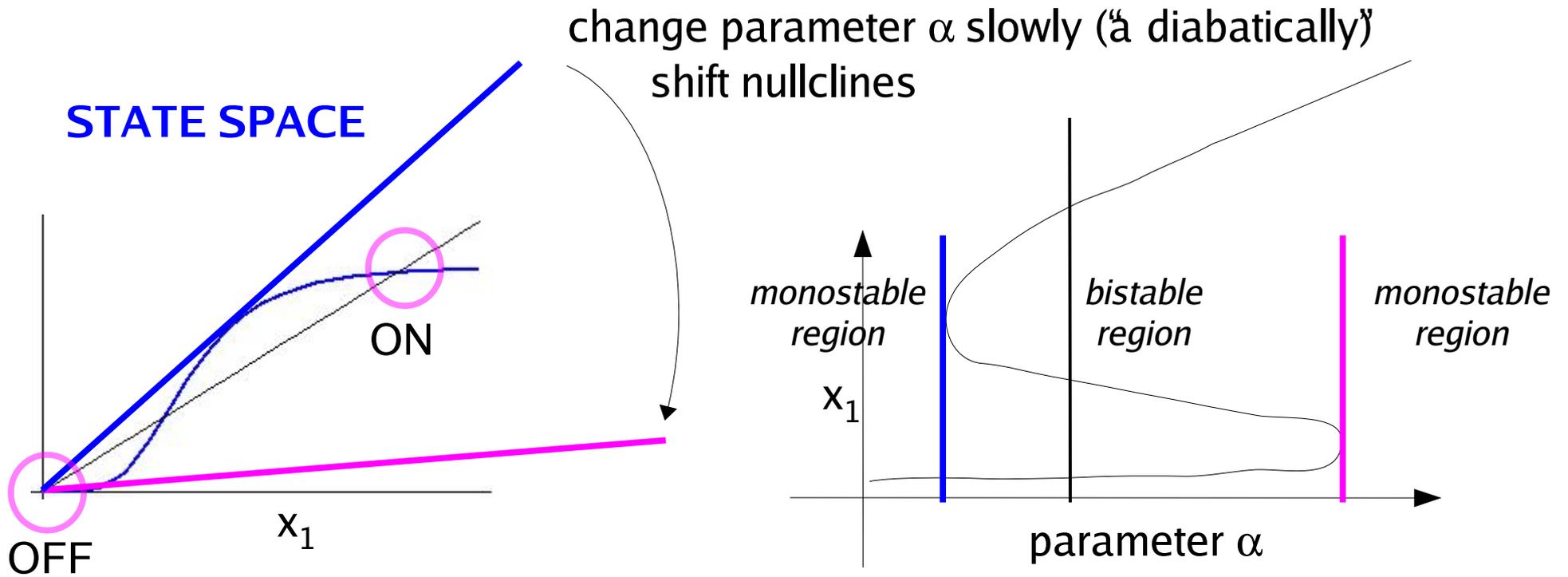
# testing bistability

method 2:

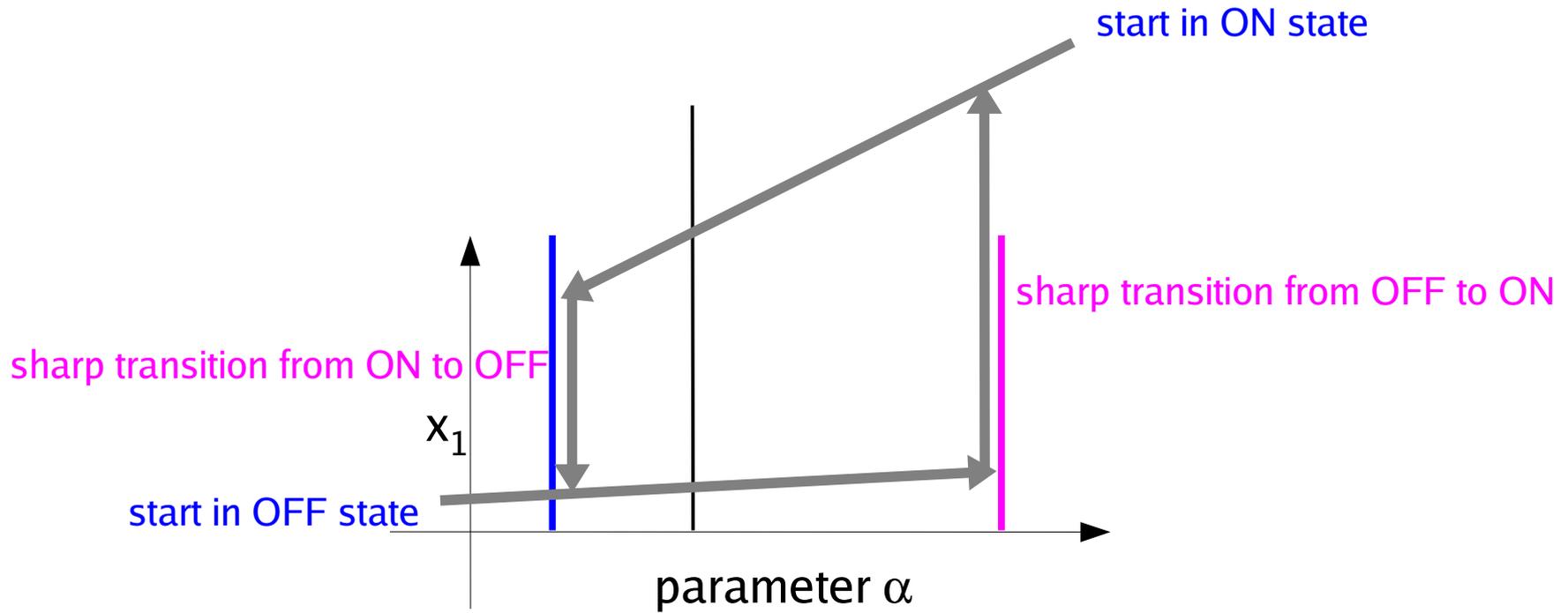
*change the parameter values and show **hysteresis***



# HYSTERESIS

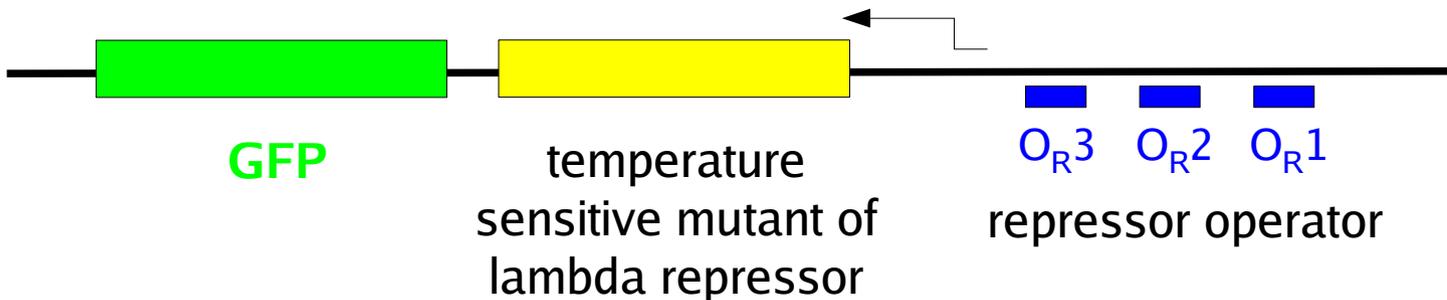


A hysteretic cycle is evidence of creation/annihilation of stable **attractors**



# experimental detection of bistability in phage lambda

engineered phage lambda autoregulatory loop

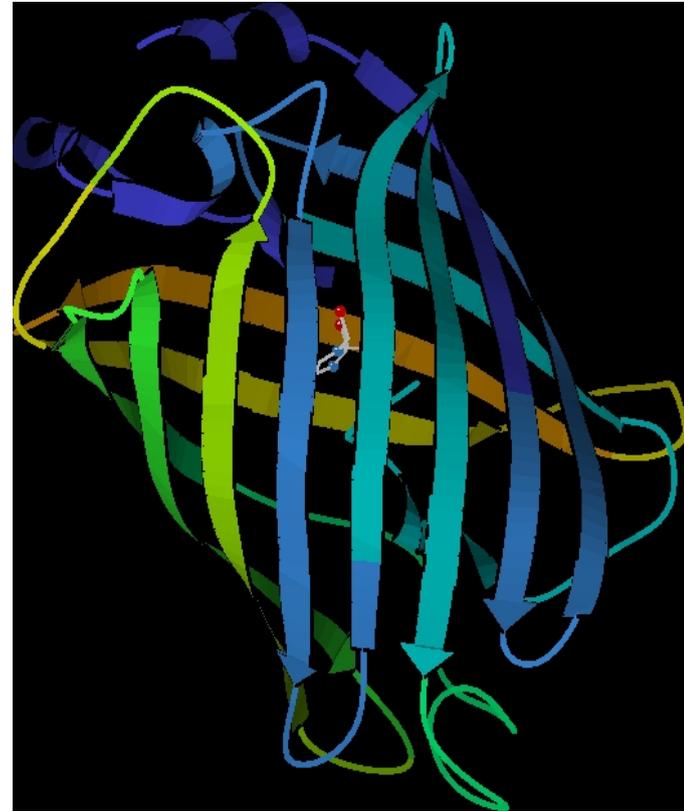


transfected into E coli

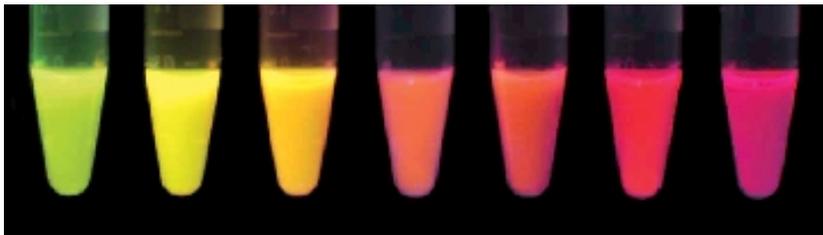
Farren Isaacs, Jeff Hasty, Charles Cantor and James Collins,  
*"Prediction and measurement of an autoregulatory genetic module"*  
PNAS **100**:7714-9 2003



*Aequoria victoria*



*Green fluorescent protein*  
PDB 1QYQ

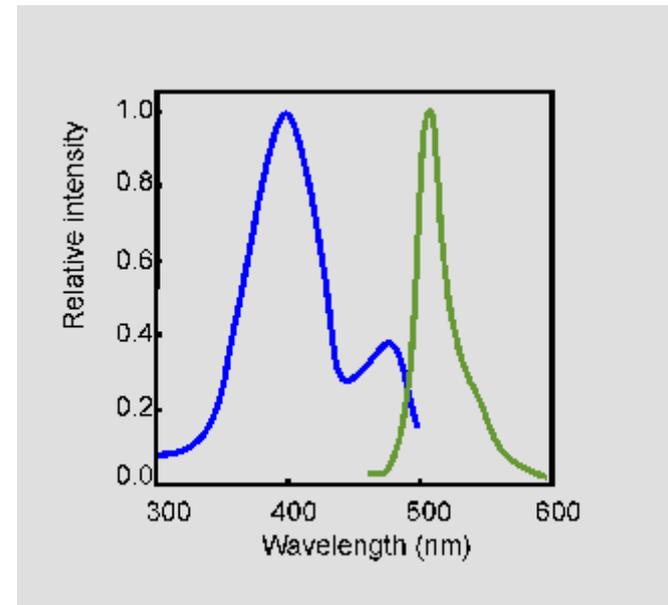
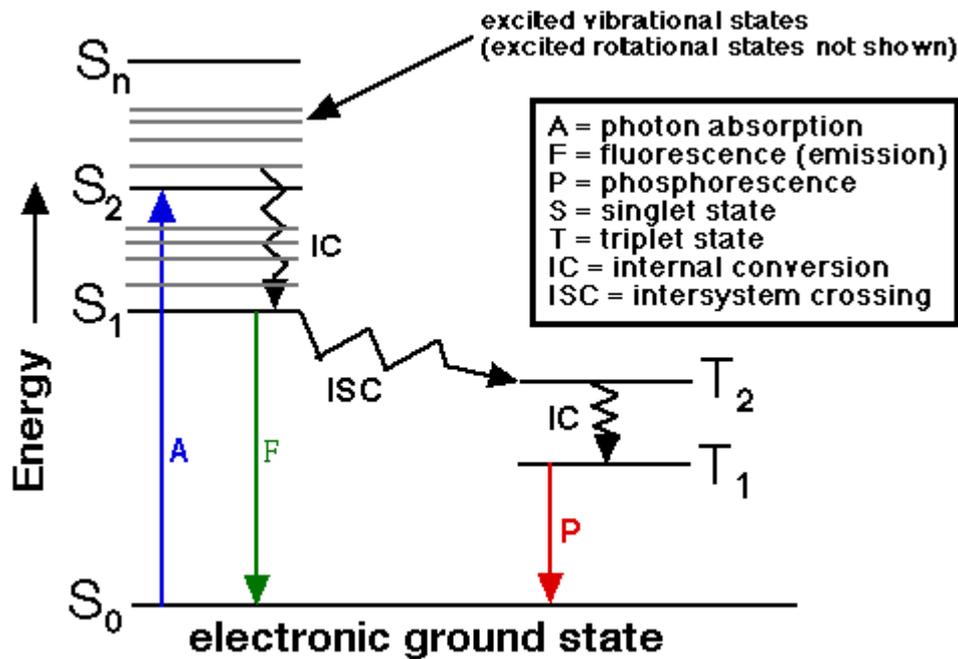
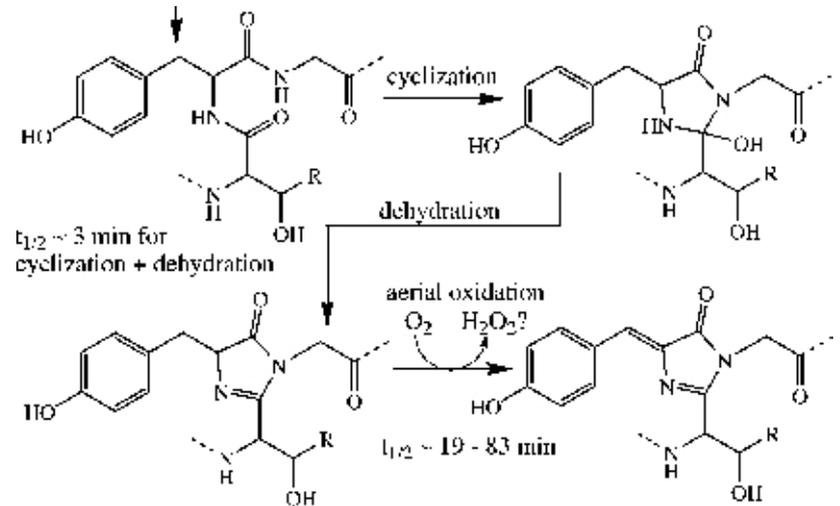


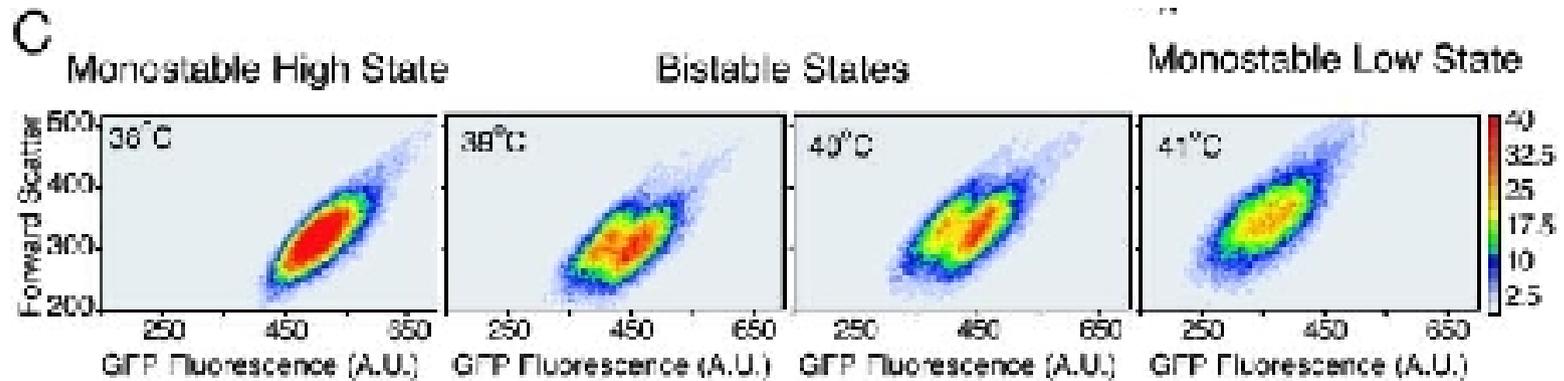
N. C. Shaner, R. E. Campbell, P.A. Steinbach, B.N.G. Giepmans, A.E. Palmer & R. Tsien  
*“Improved monomeric red, orange and yellow fluorescent proteins derived from Discosoma  
sp. red fluorescent protein,” Nature Biotech., 22:1587-72 2004*

# GFP matures post-translationally

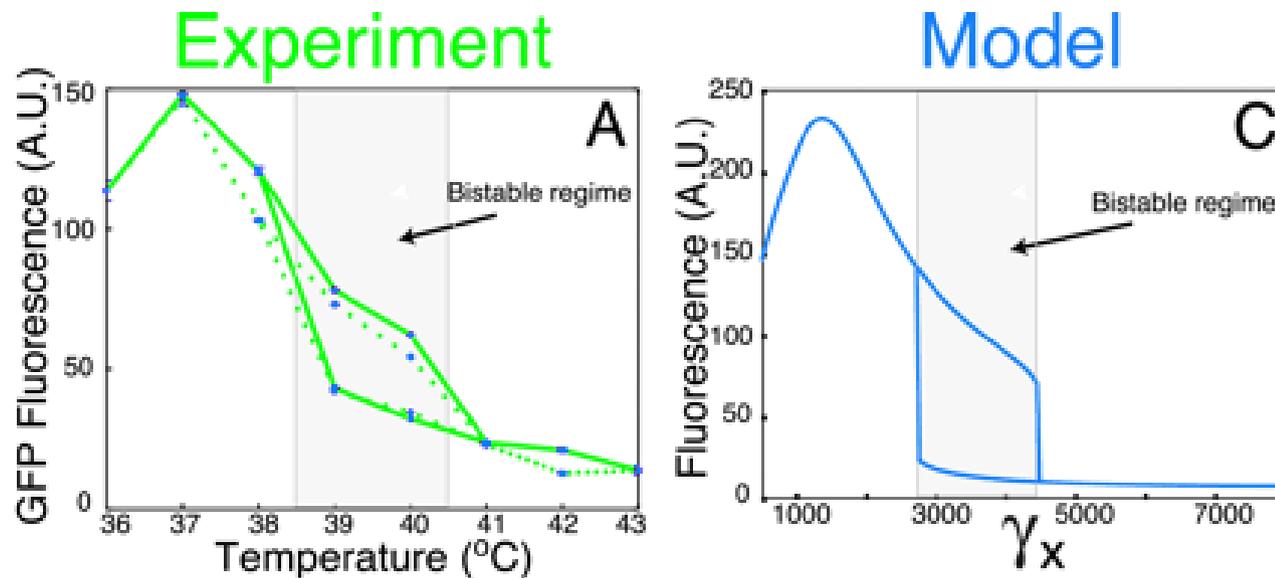
chromophore -SYG motif at residues 65-67

maturation - cyclisation, dehydration, oxidation





**biphasic** response to temperature shift

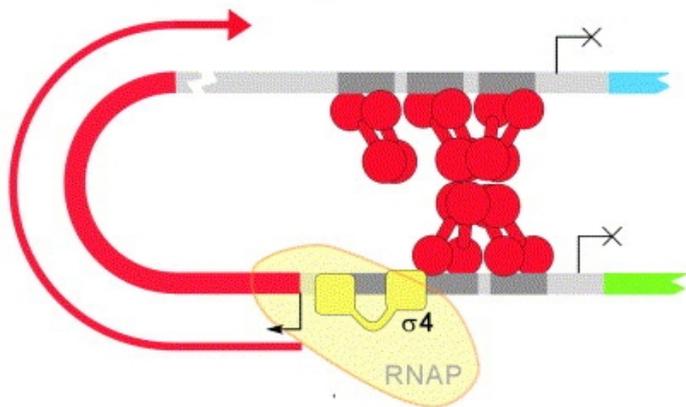


**bistable** response to temperature shift

# phage lambda is still not fully understood !!

Measured frequency of spontaneous lysis  
~  $10^{-8}$  per cell per generation  
~ once per cell per 5000 years!  
Not explained by current models

Aurell, Brown, Johanson & Sneppen  
“Stability puzzles in phage  $\lambda$ ”  
Phys Rev E 65:051914 2002



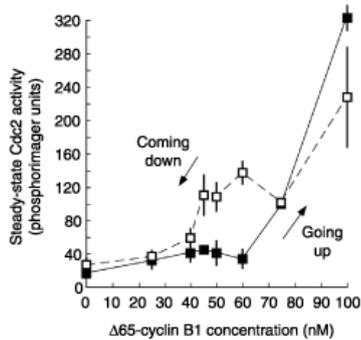
Dodd, Shearwin & Egan  
“Revised gene regulation in bacteriophage  $\lambda$ ”  
Cur Op Gen Dev 15:145-52 2005

DNA looping creates more cooperativity

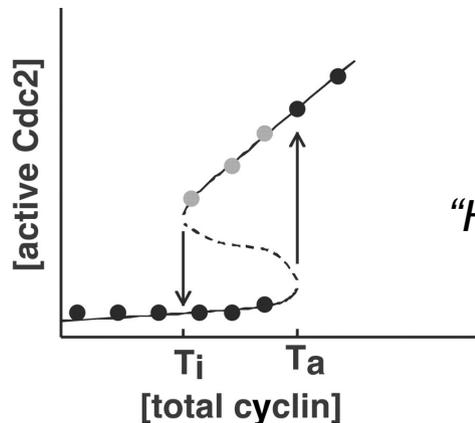
Redundancy?

Michalowski & Little  
“Positive autoregulation of *cl* is a dispensable feature of phage  $\lambda$  gene regulatory circuitry”  
J Bacteriology 187:6430-42 2005

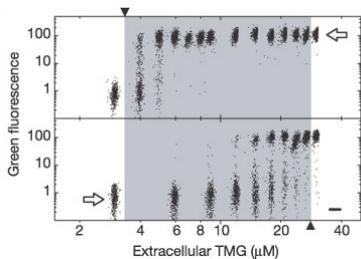
hysteresis has been widely used to test for bistability



Pomerening, Sontag & James Ferrell  
*"Building a cell cycle oscillator:  
hysteresis and bistability in the activation of CDC2"*  
Nature Cell Biology 5:346-51 2005



Sha, Moore, Chen, Lassaletta, Yi, Tyson & Sible  
*"Hysteresis drives cell-cycle transitions in Xenopus laevis egg extracts"*  
PNAS 100:975-80 2003

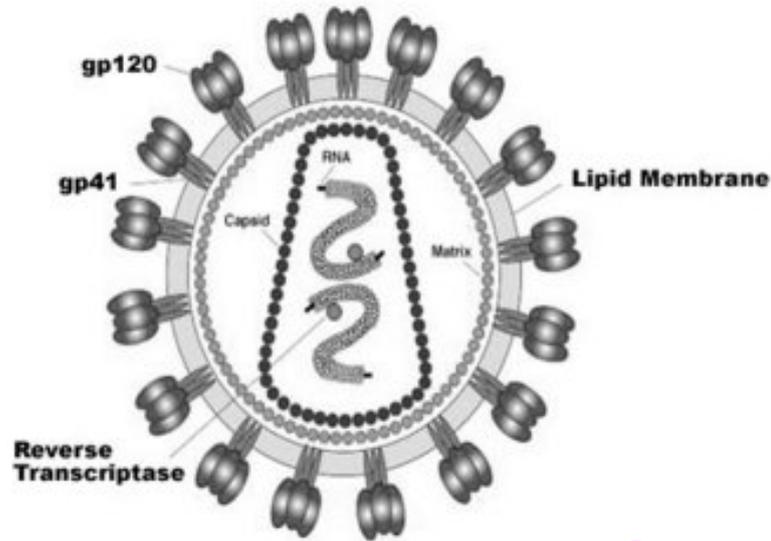


Ozbudak, Thatai, Lim, Shraiman & van Oudenaarden  
*"Multistability in the lactose utilization network of Escherichia coli"*  
Nature 427:737-40 2004

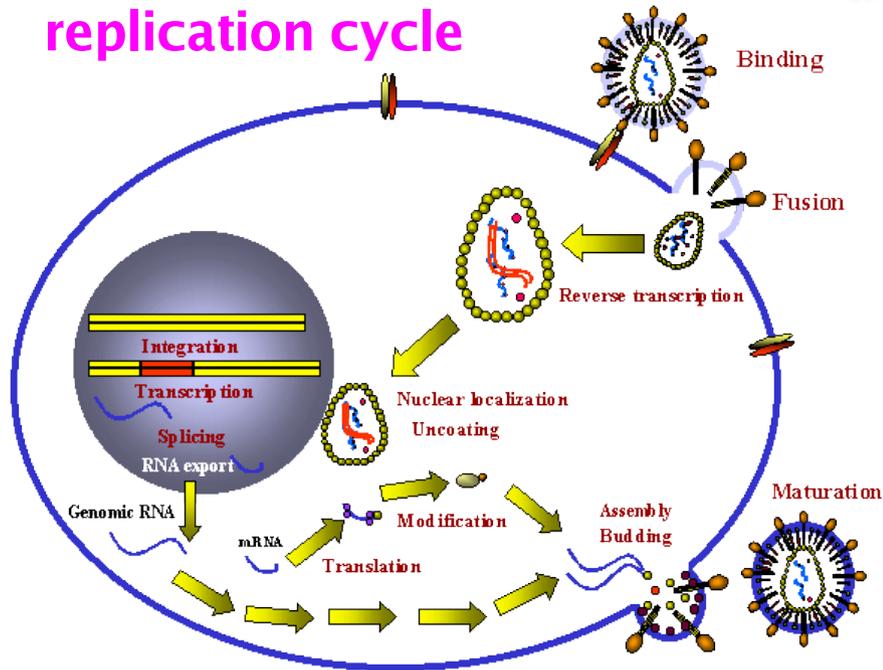
# **LATENCY SWITCH IN HIV-1**

# HIV-1

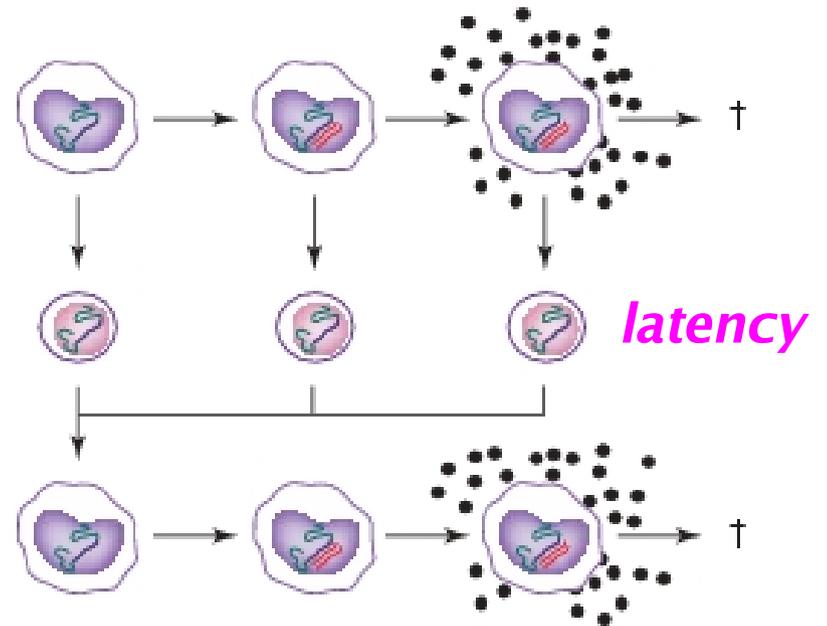
virion structure



replication cycle

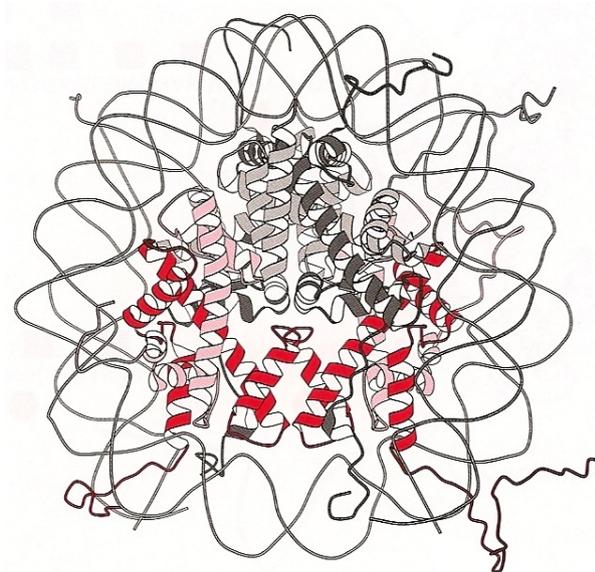
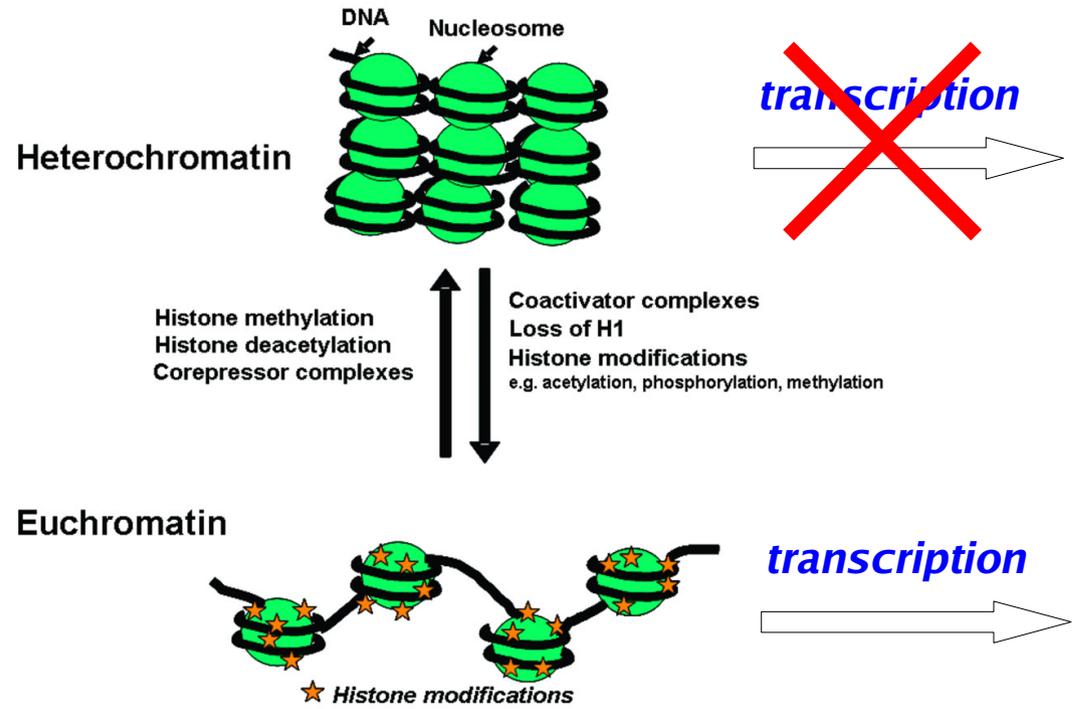
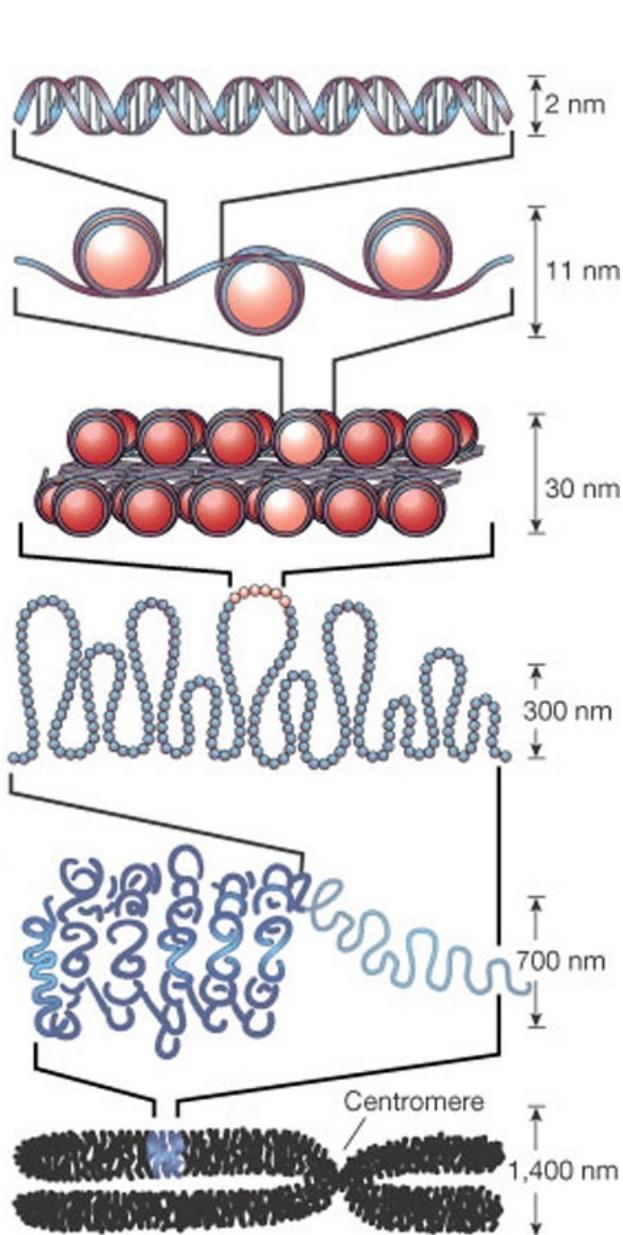


CD4+ T cell infection

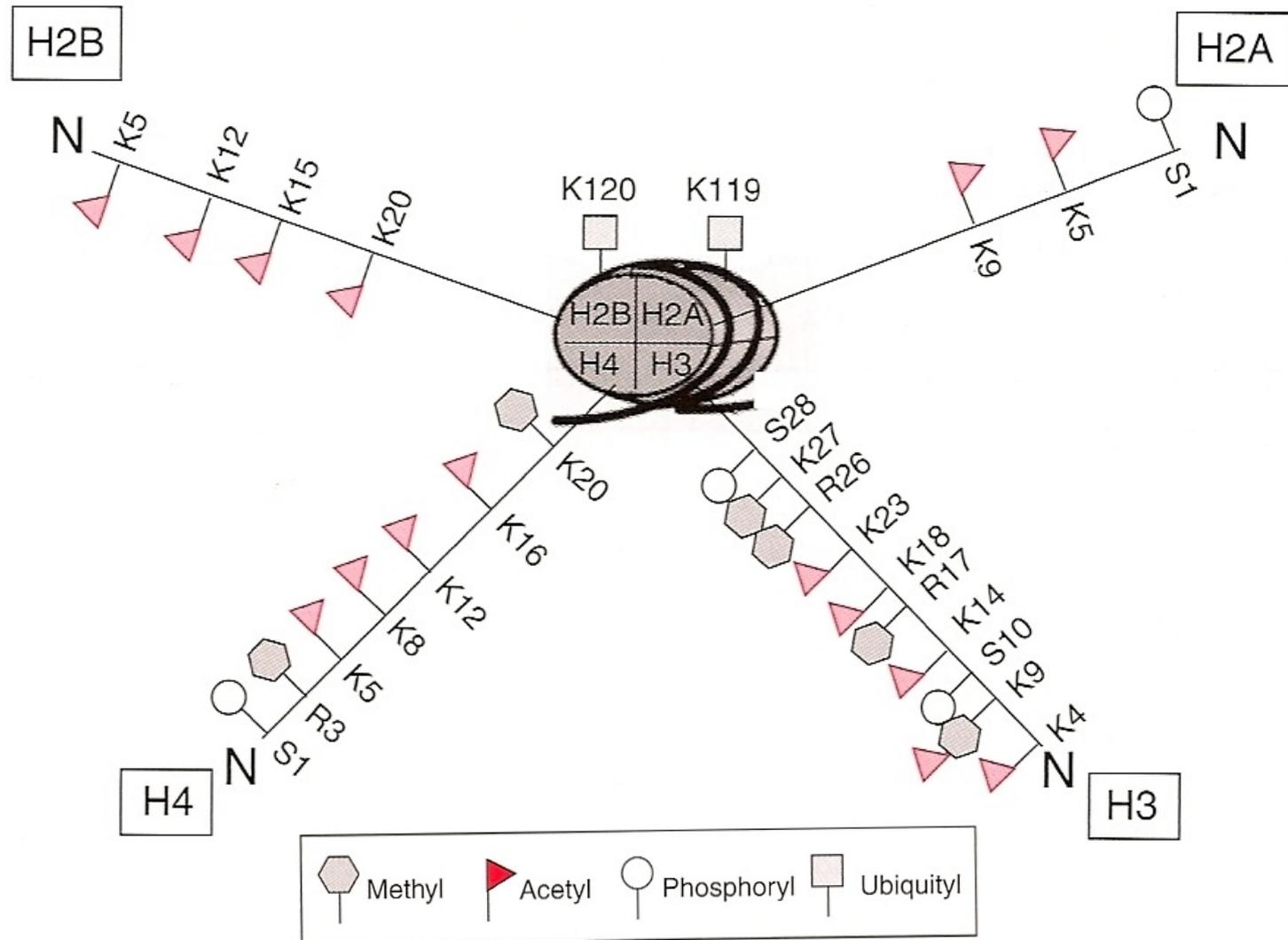


Lassen, Han, Zhou, Siliciano, Siliciano, "The multifactorial nature of HIV-1 latency," Trends Mol. Med. 10:525-31 2004

# eukaryotic gene transcription is repressed by chromatin



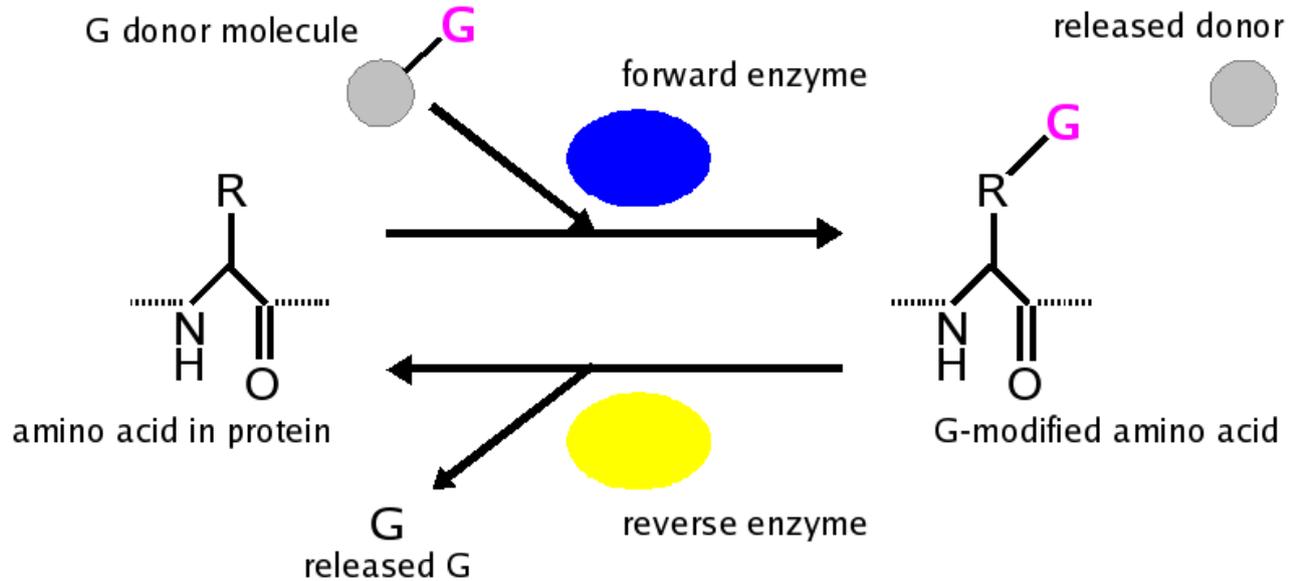
and regulated by a hypothetical “histone code”



Turner, *Decoding the nucleosome*, Cell 75:5-8 1993.

Strahl, Allis, *The language of covalent histone modifications*, Nature 403:41-53 2000

# most proteins are post-translationally modified

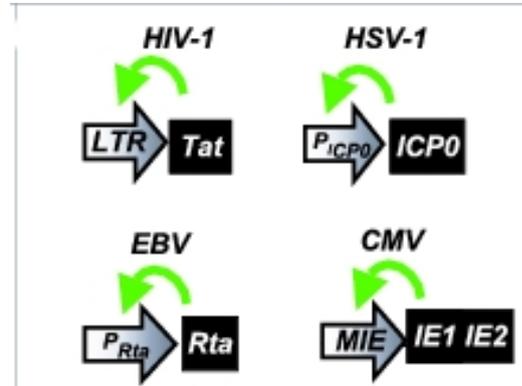


Modification	Modifier	Donor	Modified residue
phosphorylation	$\text{PO}_3^{2-}$	ATP	S, T, Y (H, D in bacteria)
sulfation	$\text{SO}_3^-$	PAPS	Y† (extracellular)
methylation	$\text{CH}_3$	SAM	E, K(1-3)†, R(1-2)†
acetylation	$\text{CH}_3\text{CO}$	AcCoA	K
ubiquitylation	Ubiquitin	-	K
ubiquitylation-like	SUMO, Nedd8, ...	-	K

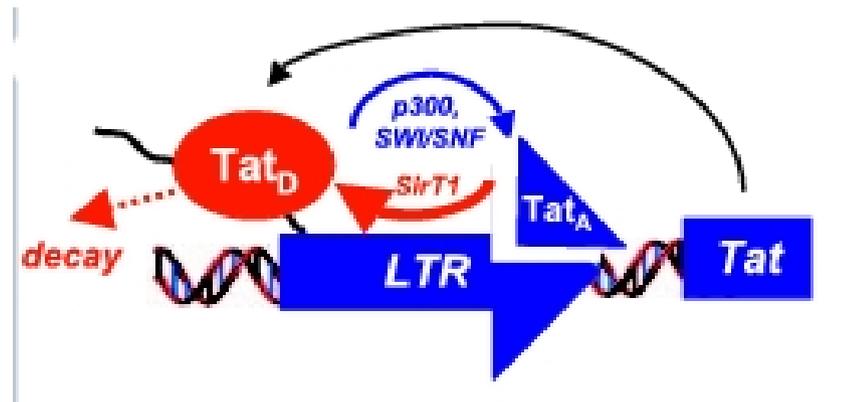
† = reverse enzymes not known

latent viruses use transcriptional activators to initiate lysis

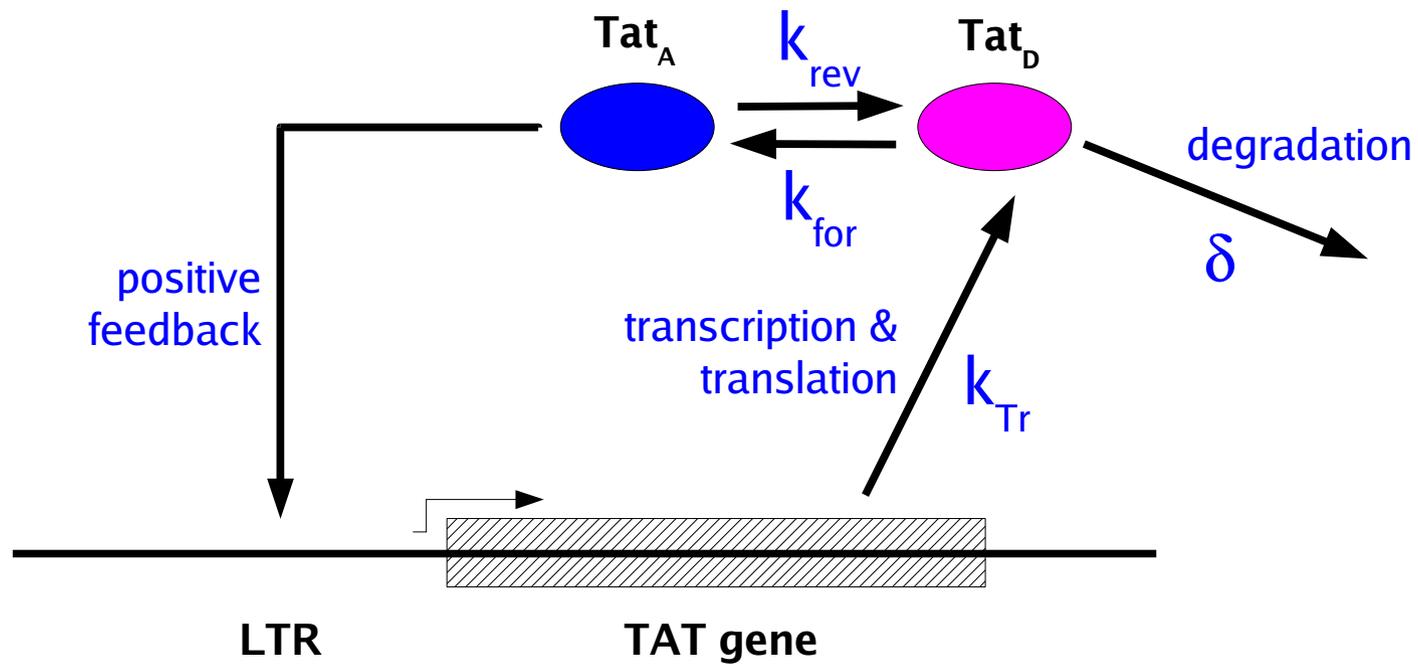
stable off states (latency) are not maintained by cooperativity



### HIV-1 autoregulatory loop



Leor Weinberger and Thomas Shenk, *A n HIV feedback resistor: auto-regulatory circuit deactivator and noise buffer,*  
PLoS Biol. 5:e91 2007



## linear model

$$\begin{aligned} \frac{d}{dt} (Tat_D) &= -k_{for} \cdot Tat_D + (k_{rev} + k_{Tr}) Tat_A - \delta \cdot Tat_D \\ \frac{d}{dt} (Tat_A) &= k_{for} \cdot Tat_D - k_{rev} \cdot Tat_A \end{aligned}$$

$$\frac{d}{dt} \begin{pmatrix} \text{Tat}_D \\ \text{Tat}_A \end{pmatrix} = \begin{pmatrix} -k_{for} - \delta & k_{rev} + k_{Tr} \\ k_{for} & -k_{rev} \end{pmatrix} \begin{pmatrix} \text{Tat}_D \\ \text{Tat}_A \end{pmatrix}$$

$$\text{Tr} = -(k_{for} + \delta + k_{rev}) < 0$$

$$\text{det} = \delta k_{rev} - k_{for} k_{Tr}$$

*condition for stability of the off state*

$$\delta k_{rev} > k_{for} k_{Tr}$$

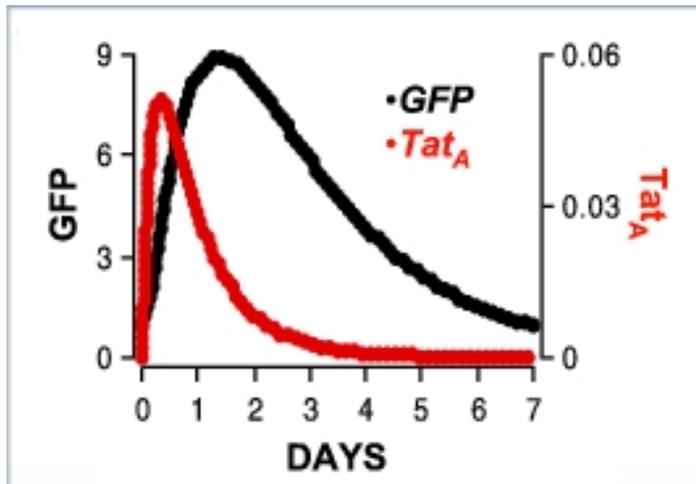
## engineered HIV-1 autoregulatory loop



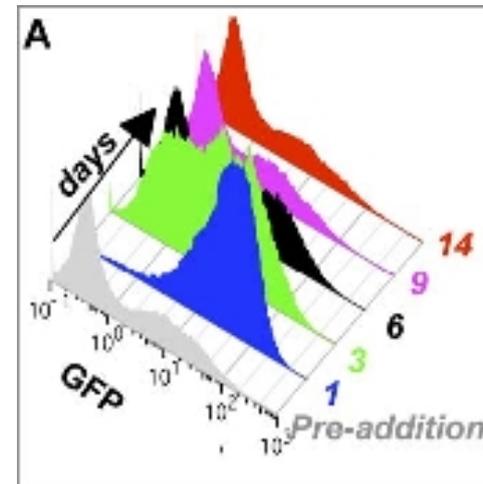
transfected into Jurkat cells (a T cell cancer line)

Weinberger, Burnett, Toettcher, Arkin, Schaffer, *“Stochastic gene expression in a lentiviral positive-feedback loop,”*  
Cell 122:169-82 2005

## addition of a pulse of Tat<sub>D</sub>



simulation



data